

```

u = 0.5cm;
angle_radius = 8pt;
penthick = .3pt;
marksize = 4pt;
defaultscale := .7;
verbatim
\font\teni=cmmi10 scaled 700
\textfont1\teni
\textfont0\sevenrm
etex

input macros

beginfig(0);
draw(0, 0) -- (10u, 0);
pair za, zb, zc;
za = (u, 0);
zb = (4u, 0);
zc = (9u, 0);
pickup pencircle scaled 4pt;
dotlabel top(btex $A$ etex, za);
dotlabel top(btex $B$ etex, zb);
dotlabel top(btex $C$ etex, zc);
endfig;

beginfig(1);
draw(0, 0) -- (10u, 0);
dotlabel top(btex $A$ etex, za);
dotlabel top(btex $B$ etex, zb);
dotlabel top(btex $C$ etex, zc);
label bot(btex $3$ etex, .5[za, zb]);
label bot(btex $5$ etex, .5[zb, zc]);
endfig;

beginfig(2);
draw(0, 0) -- (7u, 0);
pair zaa, zbb, zcc;
zaa = (4u, 0);
zbb = (u, 0);
zcc = (6u, 0);
dotlabel top(btex $A$ etex, zaa);
dotlabel top(btex $B$ etex, zbb);
dotlabel top(btex $C$ etex, zcc);
label bot(btex $3$ etex, .5[zbb, zaa]);
label bot(btex $2$ etex, .5[zaa, zcc]);
endfig;

beginfig(3);
draw(0, 0) -- (9.6u, 0) -- (9.6u, 2u) -- (0, 2u) -- cycle;
draw(0.4u, 2u) -- (0.4u, 1.4u);
draw(6u, 2u) -- (6u, 1.4u);
draw(9.2u, 2u) -- (9.2u, 1.4u);
pickup pencircle scaled 4pt;
label bot(btex $0$ etex, (0.4u, 1.4u));
label bot(btex $7$ etex, (6u, 1.4u));

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```
label bot(btex $11$ etex, (9.2u, 1.4u));
endfig;
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```
beginfig(4);
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```
pair za, zb, zc, zaa, zcc, zab, zbc;
za = (u, 2u);
zb = (3u, 2u);
zc = (10u, 2u);
zaa = (u, 0.4u);
zcc = (10u, 0.4u);
zab = .5[za, zb];
zbc = .5[zb, zc];
pickup pencircle scaled 0.2pt;
draw(0, 2u) -- (11u, 2u);
draw za -- (u, 0);
draw zb -- (3u, 1.8u);
draw zc -- (10u, 0);
drawdblarrow zaa .. zcc;
draw zab{dir -30} .. zbc dashed evenly;
pickup pencircle scaled 4pt;
label top(btex $A$ etex, za);
label top(btex $B$ etex, zb);
label top(btex $C$ etex, zc);
label top(btex $5$ etex, .5[zaa, zcc]);
endfig;
```

```
beginfig(5);
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```
pair za, zx, zb;
picture house;
za = (u, 0);
zx = (7u, 0);
zb = (11u, 0);
draw(0.5u, 0.2u) -- (1.5u, 0.2u) -- (1.5u, 1.2u) -- (0.5u, 1.2u) -- cycle;
draw(0.3u, 0.9u) -- (u, 2u) -- (1.7u, 0.9u);
house = currentpicture;
draw house shifted (10u, 0);
draw(0, 0) -- (12u, 0);
pickup pencircle scaled 4pt;
dotlabel bot(btex $A$ etex, za);
dotlabel bot(btex $x$ etex, zx);
dotlabel top(btex $?$ etex, zx);
dotlabel bot(btex $B$ etex, zb);
endfig;
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```
beginfig(6);
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```
draw(0, 0) -- (12u, 0);
dotlabel top(btex $A$ etex, za);
dotlabel top(btex $x$ etex, zx);
dotlabel top(btex $B$ etex, zb);
dotlabel bot(btex $AX+XB=AB$ etex, zx);
endfig;
```

```
beginfig(7);
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```
pair za, zb, zc, zd;
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draw(0, 0) -- (12u, 0);
za = (u, 0);
zb = (4.33u, 0);
zc = (7.33u, 0);
zd = (11u, 0);
dotlabel bot(btex  $A$  etex, za);
dotlabel bot(btex  $B$  etex, zb);
dotlabel bot(btex  $C$  etex, zc);
dotlabel bot(btex  $D$  etex, zd);
draw za{dir -30} .. zd;
draw zb{dir -30} .. zc;
endfig;

beginfig(8);
pair za, zx, zb;
picture templ;
draw(0, 0) -- (7u, 0);
za = (u, 0);
zb = (6u, 0);
zx = (3u, 0);
dotlabel top(btex  $100$  etex, za);
dotlabel top(btex  $50$  etex, zb);
templ = currentpicture;
label bot(btex  $A$  etex, za);
label bot(btex  $B$  etex, zb);
endfig;

beginfig(9);
draw templ;
draw za{dir -40} .. zx & zx{dir -30} .. zb;
dotlabel bot(btex  $x$  etex, zx);
label bot(btex  $x$  etex, (2u, -0.5u));
label bot(btex  $3-x$  etex, (4.5u, -0.4u));
endfig;

beginfig(10);
pair za, zb, zc;
za = (2.8u, 2.8u);
zb = (3.4u, 2.2u);
zc = (4u, 0);
draw(0, 0) -- za;
draw(0, 0) -- zb dashed evenly;
draw(0, 0) -- zc;
label bot(btex  $0$  etex, (0, 0));
label urt(btex  $A$  etex, za);
label urt(btex  $B$  etex, zb);
label bot(btex  $C$  etex, zc);
endfig;

beginfig(11);
pair a, b, c, d, e, f;
a = (0, 4u);
b = (0, 0);
c = (4u, 0);
draw a -- b -- c;

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mark_rt_angle(c, b, a);
label urt(btex $90$ etex, (7, 7));
d = (5u, 0);
e = (7u, 0);
f = (9u, 0);
draw d -- e -- f;
dotlabel(btex $$ etex, e);
mark_ang(f, e, d, angle_radius);
label urt(btex $180$ etex, (7u, 7));
endfig;

beginfig(12);
pair d, e, f, g, h;
d = (-4u, 0);
e = (0, 0);
f = (4u, 0);
draw d -- e -- f;
dotlabel bot(btex $$ etex, e);
for i = 1 upto 4:
  g := f rotated 40;
  draw e -- g;
  mark_ang(f, e, g, angle_radius);
  f := g;
endfor;
label urt(btex $40$ etex, (.5u, .01u));
label urt(btex $40$ etex, (.2u, .7u));
label ulft(btex $40$ etex, (.3u, .8u));
label ulft(btex $40$ etex, (-.5u, .4u));
label ulft(btex $20$ etex, (-1.3u, -.1u));
endfig;

beginfig(13);
pair c, d, e, f, g;
c = (0, 0);
d = (4u, 2.5u);
e = (0, 2.5u);
f = (4u, 0);
draw c -- d;
draw e -- f;
g = whatever[c, d] = whatever[e, f];
mark_ang(f, g, d, angle_radius);
label rt(btex $41$ etex, g shifted (.5u, 0));
endfig;

beginfig(14);
pair c, d, e, f, g;
c = (0, 0);
d = (4u, 2.5u);
e = (0, 2.5u);
f = (4u, 0);
draw c -- d;
draw e -- f;
g = whatever[c, d] = whatever[e, f];
mark_ang(f, g, d, angle_radius);
mark_ang(e, g, c, angle_radius);

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```

label rt(btex $41$ etex,  $g$  shifted (.5u, 0));
label lft(btex $41$ etex,  $g$  shifted (-.5u, 0));
label top(btex $139$ etex,  $g$  shifted (0, .2u));
label bot(btex $139$ etex,  $g$  shifted (0, -.2u));
endfig;

beginfig(15);
pair  $c, d, e, f, g$ ;
 $c = (-2u, 0)$ ;
 $d = (0, 0)$ ;
 $e = (2u, 0)$ ;
 $f = (2u, 2u)$ ;
draw  $c$  --  $e$ ;
draw  $d$  --  $f$ ;
mark_ang( $e, d, f$ , angle_radius);
mark_angtwice( $f, d, c$ , angle_radius);
label ulft(btex $smejnie$ etex,  $f$ );
label urt(btex $ygli$ etex,  $f$ );
drawarrow reverse((- .7u, .5u){dir 120} .. (-.5u, 2u));
drawarrow reverse(.7u, .2u){dir 20} .. (3u, 2u));
endfig;

beginfig(16);
pair  $c, d, e, f, g$ ;
 $c = (0, 0)$ ;
 $d = (4u, 2.5u)$ ;
 $e = (0, 2.5u)$ ;
 $f = (4u, 0)$ ;
draw  $c$  --  $d$ ;
draw  $e$  --  $f$ ;
 $g = \text{whatever}[c, d] = \text{whatever}[e, f]$ ;
mark_ang( $f, g, d$ , angle_radius);
mark_ang( $e, g, c$ , angle_radius);
label top(btex $vertikalnie$ etex,  $d$ );
label lrt(btex $ygli$ etex,  $d$ );
drawdot(2.5u, 2.5u);
drawdot(1.2u, 1.2u);
drawdot(4u, 1.8u);
drawdot(2.8u, 1.2u);
drawarrow reverse((1.2u, 1.2u){dir 100} .. (2.5u, 2.5u));
drawarrow reverse((2.8u, 1.2u){dir 20} .. (4u, 1.8u));
endfig;

beginfig(17);
interim defaultscale := 1.5;
 $z_0 = (0, 0)$ ;
 $z_1 = -z_3 = (4u, 0)$ ;
 $z_2 = -z_4 = (0, 4u)$ ;
path  $p$ ;
pair clock[];
 $p = z_1 .. z_2 .. z_3 .. z_4 .. \text{cycle}$ ;
draw  $p$ ;
for  $i = 0$  upto 11:
    markpoint( $p, i/3$ );
endfor;

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```
label lft(btex $$$ etex, z_1 shifted (-.5u, 0));
endfig;
```

```
beginfig(18);
z_0 = (0, 0);
z_1 = (4u, 0);
z_2 = (2u, 3u);
draw z_1 -- z_0 -- z_2;
label rt(btex $$A$ etex, z_2);
label lft(btex $0$ etex, z_0);
label rt(btex $C$ etex, z_1);
mark_ang(z_1, z_0, z_2, angle_radius);
z_3 = z_1 rotated -20;
z_4 = z_2 rotated -20;
draw z_3 -- z_0 -- z_4;
mark_ang(z_3, z_0, z_4, 10);
label rt(btex $$B$ etex, z_4);
label rt(btex $$D$ etex, z_3);
endfig;
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```
beginfig(19);
z_0 = (0, 0);
z_1 = (4u, 0);
z_2 = z_1 rotated 20;
z_3 = z_1 rotated -20;
draw z_0 -- z_2;
draw z_0 -- z_1 dashed evenly;
label rt(btex $bissectrica$ etex, z_1);
draw z_0 -- z_3;
mark_ang(z_1, z_0, z_2, angle_radius);
mark_ang(z_3, z_0, z_1, 10);
endfig;
```

```
beginfig(20);
z_1 = (2u, u);
z_2 = (1.7u, -u);
z_3 = (-1.8u, .8u);
z_4 = (-2u, -1.2u);
z_0 = whatever[z_1, z_4] = whatever[z_2, z_3];
draw z_1 -- z_4;
draw z_2 -- z_3;
ang_and_bis(z_2, z_0, z_1);
ang_and_bistwice(z_1, z_0, z_3);
ang_and_bis(z_3, z_0, z_4);
ang_and_bistwice(z_4, z_0, z_2);
endfig;
```

```
beginfig(21);
z_0 = (0, 0);
z_1 = -z_3 = (2u, 0);
z_2 = (-2u, 2u);
draw z_1 -- z_3;
draw z_0 -- z_2;
ang_and_bis(z_2, z_0, z_3);
ang_and_bistwice(z_1, z_0, z_2);
```

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endfig;

beginfig(22);
 $z_0 = (0, 0);$ 
 $z_1 = (0, 2u);$ 
draw  $z_0$  --  $z_1$ ;
pair  $rot[]$ ;
 $rot[1] = z_1$ ;
for  $i = 1$  upto 5:
   $rot[i + 1] = rot[i]$  rotated 72;
  draw  $z_0$  --  $rot[i + 1]$ ;
   $mark\_ang(rot[i], z_0, rot[i + 1], angle\_radius);$ 
endfor;
endfig;

beginfig(23);
 $z_0 = (0, 0);$ 
 $z_1 = (0, 2u);$ 
draw  $z_0$  --  $z_1$ ;
pair  $rot[]$ ;
 $rot[1] = z_1$ ;
for  $i = 1$  upto 5:
   $rot[i + 1] = rot[i]$  rotated 72;
  draw  $z_0$  --  $rot[i + 1]$ ;
endfor;
draw  $(-2u, 0)$  --  $(2u, 0)$  dashed evenly;
label ulft(btex  $\$1\$$  etex,  $(-.05u, .2u)$ );
label urt(btex  $\$2\$$  etex,  $(.05u, .2u)$ );
label rt(btex  $\$3\$$  etex,  $(1.5u, .3u)$ );
label lrt(btex  $\$4\$$  etex,  $(.5u, 0)$ );
label bot(btex  $\$5\$$  etex,  $(0, -.2u)$ );
label llft(btex  $\$6\$$  etex,  $(-.5u, 0)$ );
label lft(btex  $\$7\$$  etex,  $(-1.5u, .3u)$ );
endfig;

beginfig(24);
 $z_0 = (0, 0);$ 
 $z_1 = -z_3 = (2u, u);$ 
 $z_2 = -z_4 = (2u, -u);$ 
draw  $z_1$  --  $z_3$ ;
draw  $z_2$  --  $z_4$ ;
 $mark\_ang(z_2, z_0, z_1, 11pt);$ 
 $mark\_angtwice(z_1, z_0, z_4, angle\_radius);$ 
 $mark\_ang(z_4, z_0, z_3, 11pt);$ 
 $mark\_angtwice(z_3, z_0, z_2, angle\_radius);$ 
label rt(btex  $\alpha$  etex,  $z_0$  shifted  $(.6u, 0)$ );
label bot(btex  $\beta$  etex,  $z_0$  shifted  $(0, 1.6u)$ );
label lft(btex  $\alpha$  etex,  $z_0$  shifted  $(-.6u, 0)$ );
label top(btex  $\beta$  etex,  $z_0$  shifted  $(0, -1.6u)$ );
endfig;

beginfig(25);
 $z_0 = (0, 0);$ 
 $z_1 = (2u, 0);$ 
 $z_2 = z_1$  rotated 45;

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z3 = z1 rotated 90;
draw z1 -- z0;
draw z2 -- z0;
draw z3 -- z0;
ang_and_bis(z1, z0, z2);
ang_and_bistwice(z2, z0, z3);
endfig;

beginfig(26);
z0 = (0, 0);
pair za, zb, zc;
za = (2u, 0);
z1 = za rotated 30;
for i = 0 upto 3:
    z[i + 2] = z[i] rotatedaround(z[i + 1], -120);
endfor;
path p, so, ss;
p = z0 -- z1 -- z2 -- z3 -- z4 -- z5 -- cycle;
z2 = z4 shifted zb;
show zb;
for i = 0 upto 3:
    draw p shifted (i * zb);
endfor;
z5 = z3 shifted zc;
so = p shifted zc;
for i = 0 upto 4:
    draw so shifted (i * zb);
endfor;
ss = p shifted (0, -6u);
for i = 0 upto 3:
    draw ss shifted (i * zb);
endfor;
endfig;

beginfig(27);
pair za, zb, zc, zd;
za = (0, 0);
zc = (3u, 0);
zb = (2u, u);
draw za -- zc;
draw za -- zb dashed evenly;
draw zb -- zc dashed evenly;
dotlabel bot(btex  $\$A\$$  etex, za);
dotlabel top(btex  $\$B\$$  etex, zb);
dotlabel bot(btex  $\$C\$$  etex, zc);
label top(btex $prjamoj pyt' (A->C)$ etex, (-u, -1.7u));
label top(btex $koro4e neprjamogo (A->B->C)$ etex, (-u, -2.4u));
endfig;

beginfig(28);
pair za, zb, zc, zd;
za = (0, 0);
zc = (3u, 0);
zb = (2u, u);
path p;

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p = za -- zb -- zc -- cycle;
draw p;
tr(p, 45);
dotlabel bot(btex  $A$  etex, za);
dotlabel top(btex  $B$  etex, zb);
dotlabel bot(btex  $C$  etex, zc);
endfig;

beginfig(29);
pair za, zb, zc, zd;
za = (0, 0);
zb = (u, 2u);
zc = (2.5u, 2u);
zd = (3u, 0);
draw za -- zb -- zc -- zd dashed evenly;
draw za -- zd;
dotlabel bot(btex  $A$  etex, za);
dotlabel ulft(btex  $B$  etex, zb);
dotlabel urt(btex  $C$  etex, zc);
dotlabel bot(btex  $D$  etex, zd);
endfig;

beginfig(30);
pair za, zb, zc, zd;
za = (0, 0);
zb = (u, 2u);
zc = (2.5u, 2u);
zd = (3u, 0);
draw za -- zb -- zc -- zd -- cycle;
draw za -- zc;
dotlabel bot(btex  $A$  etex, za);
dotlabel ulft(btex  $B$  etex, zb);
dotlabel urt(btex  $C$  etex, zc);
dotlabel bot(btex  $D$  etex, zd);
endfig;

beginfig(31);
z1 = (-2u, 0);
z2 = (0, 2u);
z3 = (2u, 0);
z4 = (.5u, -3u);
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z1 -- z3;
label ulft(btex  $a$  etex, .5[z1, z2]);
label urt(btex  $b$  etex, .5[z2, z3]);
label lrt(btex  $c$  etex, .5[z3, z4]);
label llft(btex  $d$  etex, .5[z4, z1]);
label bot(btex  $x$  etex, .5[z1, z3]);
endfig;

beginfig(32);
z1 = (0, 0);
z2 = (2u, 2u);
z3 = (3u, .5u);
draw z1 -- z2 -- z3;

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dotlabel(btex $$ etex, z1);
dotlabel(btex $$ etex, z2);
dotlabel(btex $$ etex, z3);
label top(btex $warnir$ etex, z2 shifted (.5u, .5u));
label ulft(btex $5$ etex, .5[z1, z2]);
label urt(btex $3$ etex, .65[z2, z3]);
drawarrow reverse(z2 shifted (.2u, 0){dir -20} .. (z2 shifted (u, .5u)));
endfig;

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```

beginfig(33);
z0 = (0, 0);
z1 = (-3u, .5u);
z2 = (-.2u, 2u);
z3 = (2u, .5u);
z4 = (-3u, -3u);
draw z1 -- z0 -- z3 dashed evenly;
draw z2 -- z0 -- z4 dashed evenly;
dotlabel lft(btex $A$ etex, z1);
dotlabel top(btex $B$ etex, z2);
dotlabel rt(btex $C$ etex, z3);
dotlabel bot(btex $D$ etex, z4);
dotlabel(btex $$ etex, z0);
label ulft(btex $?$ etex, z0 shifted (-.1u, .1u));
endfig;

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beginfig(34);
z0 = (0, 0);
z1 = (-3u, .5u);
z2 = (-.5u, 2u);
z3 = (2u, .5u);
z4 = (-.6u, -3u);
draw z1 -- z0 -- z3 dashed evenly;
draw z2 -- z0 -- z4 dashed evenly;
dotlabel lft(btex $A$ etex, z1);
dotlabel top(btex $B$ etex, z2);
dotlabel rt(btex $C$ etex, z3);
dotlabel bot(btex $D$ etex, z4);
dotlabel(btex $$ etex, z0);
draw z1 -- z3;
draw z2 -- z4;
z5 = whatever[z1, z3] = whatever[z2, z4];
dotlabel(btex $$ etex, z5);
drawarrow z0 .. z5 shifted (.1u, -.1u);
endfig;

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beginfig(35);
z1 = (0, 0);
z2 = (u, 2u);
z3 = (3u, 0);
z4 = (1.1u, u);
z5 = whatever[z1, z4] = whatever[z2, z3];
draw z1 -- z2 -- z3 -- cycle;
draw z1 -- z4 -- z3;
draw z4 -- z5 dashed evenly;
label lft(btex $A$ etex, z1);

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label top(btex $$ etex, z2);
label rt(btex $$ etex, z3);
dotlabel top(btex $$ etex, z4);
label urt(btex $$ etex, z5);
endfig;

beginfig(36);
z1 = (0, 0);
z2 = (u, 2u);
z3 = (3.5u, 1.5u);
z4 = (3u, -u);
z5 = (4u, .5u);
drawarrow z1 .. (.5[z1, z3]);
draw .5[z1, z3] -- z3;
draw z1 -- z2 -- z4 -- z5 -- z3 dashed evenly;
dotlabel(btex $$ etex, z1);
dotlabel(btex $$ etex, z2);
dotlabel(btex $$ etex, z3);
dotlabel(btex $$ etex, z4);
dotlabel(btex $$ etex, z5);
endfig;

beginfig(37);
z1 = (0, 0);
z2 = (-1.7u, .5u);
z3 = (-2.2u, 2.2u);
z4 = (-.8u, 3.5u);
z5 = (.5u, 3.2u);
z6 = (1.8u, 2u);
z7 = (u, .3u);
z8 = (-u, -.5u);
z9 = (-.3u, 4u);
z10 = whatever[z8, z9] = whatever[z1, z2];
z11 = whatever[z8, z9] = whatever[z4, z5];
path q;
q = z10 -- z2 -- z3 -- z4 -- z11 -- cycle;
tr(q, 45);
draw z1 -- z2 -- z3 -- z4 -- z5 -- z6 -- z7 -- cycle;
draw z8 -- z9;
endfig;

beginfig(38);
z1 = (0, 0);
z2 = (0, 2u);
z3 = (u, 2u);
z4 = (u, u);
z5 = (2u, u);
z6 = (2u, 0);
draw z1 -- z2 -- z3 -- z4 -- z5 -- z6 -- cycle;
grid(2, 2);
endfig;

beginfig(39);
z1 = (0, 3u);
z2 = (0, 5u);

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```

z3 = (u, 5u);
z4 = (u, 4u);
z5 = (2u, 4u);
z6 = (2u, 3u);
path p;
p = z1 -- z2 -- z3 -- z4 -- z5 -- z6 -- cycle;
draw p;
draw z1 -- z4;
draw p shifted (4u, 0);
draw z4 shifted (4u, 0) -- .5[z1, z2] shifted (4u, 0);
draw z4 shifted (4u, 0) -- .5[z1, z6] shifted (4u, 0);
path qo, qs, qt;
qo = .5[z1, z2] -- z4 shifted (-.5u, 0) -- .5[z3, z4] shifted (-.5u, 0) -- .5[z3, z4];
qs = z4 shifted (-.5u, 0) -- .5[z5, z6] shifted (-1.5u, 0) -- .5[z5, z6] shifted (-u, 0) -- .5[z6, z1];
qt = .5[z5, z6] shifted (-u, 0) -- .5[z5, z6] shifted (-.5u, 0) -- .5[z4, z5];
draw p shifted (0, -3u);
draw qo shifted (0, -3u);
draw qs shifted (0, -3u);
draw qt shifted (0, -3u);
z7 = .75[z1, z2] shifted (-.2u, -3u);
z8 = z7 shifted (2.4u, 0);
z9 = .75[z1, z6] shifted (0, -3.1u);
z10 = z9 shifted (0, 2.3u);
pickup pencircle scaled .15pt;
draw z7 -- z8 dashed evenly shifted (.1u, 0);
draw (z7 -- z8) shifted (0, -u) dashed evenly shifted (.1u, 0);
draw z9 -- z10 dashed evenly;
draw (z9 -- z10) shifted (-u, 0) dashed evenly;
grid(6, 5);
endfig;

beginfig(40);
z1 = (0, 0);
z2 = (0, 2u);
z3 = (2u, 0);
path p;
p = z1 -- z2 -- z3 -- cycle;
draw p;
grid(2, 2);
endfig;

beginfig(41);
z1 = (0, 0);
z2 = (0, 4u);
z3 = (4u, 4u);
z4 = (4u, 0);
path p;
p = (u, 2u) -- (u, 3u) -- (3u, 3u) -- (3u, 0) -- (2u, 0) -- (2u, 2u) -- cycle;
draw p;
draw z1 -- z2 -- z3 -- z4 -- cycle;
grid(4, 4);
endfig;

```

```

beginfig(42);
z1 = (0, 0);
z2 = (0, 4u);
z3 = (4u, 4u);
z4 = (4u, 0);
path p, q, r;
p = (u, 2u) -- (u, 3u) -- (3u, 3u) -- (3u, 0) -- (2u, 0) -- (2u, 2u) -- cycle;
q = (0, 3u) -- (2u, 3u) -- (2u, u) -- (4u, u);
r = (u, 0) -- (u, 2u) -- (3u, 2u) -- (3u, 4u);
tr(p, 45);
draw q;
draw r;
draw z1 -- z2 -- z3 -- z4 -- cycle;
grid(4, 4);
endfig;

```

```

beginfig(43);
path p;
p = (0, 0) -- (0, u) -- (u, u) -- (u, 4u) -- (5u, 4u) -- (5u, u) -- (4u, u) -- (4u, 0) -- cycle;
tr(p, 45);
draw p;
grid(5, 4);
endfig;

```

```

beginfig(44);
path p;
p = (-1cm, 0) .. (0, 1cm) .. (1cm, 0);
fill p{down} .. (0, 0){-1, 2} .. {down} cycle;
draw p .. (0, -1cm) .. cycle;
endfig;

```

```

beginfig(45);
path a, b, c, d, e, f, g;
a = (0, 0) -- (.5u, 1.5u) -- (u, 0) -- cycle;
b = ((0, 0) -- (u, 1.5u) -- (u, 0) -- cycle) shifted (2u, 0);
c = ((0, 0) -- (0, u) -- (u, u) -- (u, 0) -- cycle) shifted (4u, 0);
d = ((0, 0) -- (.5u, .866u) -- (u, 0) -- cycle) shifted (0, -2u);
e = (fullcircle scaled u shifted (.5u, .5u)) shifted (2u, -2u);
f = ((0, u) -- (0, 2u) -- (u, 2u) -- (u, 4u) -- (2u, 4u) -- (2u, 3u) -- (4u, 3u) -- (4u, 2u) -- (3u, 2u) --
(3u, 0) -- (2u, 0) -- (2u, u) -- cycle) scaled 0.25 shifted (4u, -2u);
tr(a, 45);
draw a;
draw b;
draw c;
draw d;
draw e;
draw f;
endfig;

```

```

beginfig(46)
z1 = (0, 0);
z2 = (0, 2u);
z3 = (2u, 2u);
z4 = (2u, 0);
path p;

```

```

p = z1 -- z2 -- z3 -- z4 -- cycle;
draw p;
draw z1 -- z3;
draw p shifted (4u, 0);
draw (.5[z1, z4] -- .5[z2, z3]) shifted (4u, 0);
endfig;

```

```

beginfig(47);
z1 = (0, 0);
z2 = (1.5u, 2u);
z3 = (4u, 0);
draw z1 -- z2 -- z3 -- cycle;
mark_ang(z3, z1, z2, .5u);
draw_marked(z1 -- z2, 1);
draw_marked(z1 -- z3, 2);
endfig;

```

```

beginfig(48);
z1 = (0, 0);
z2 = (1.5u, 2u);
z3 = (4u, 0);
draw z1 -- z2 -- z3 -- cycle;
mark_ang(z3, z1, z2, .5u);
mark_angtwice(z2, z3, z1, .5u);
draw_marked(z1 -- z3, 1);
endfig;

```

```

beginfig(49);
z1 = (0, 0);
z2 = (1.5u, 2u);
z3 = (4u, 0);
draw z1 -- z2 -- z3 -- cycle;
draw_marked(z1 -- z2, 2);
draw_marked(z1 -- z3, 1);
draw_marked(z2 -- z3, 3);
endfig;

```

```

beginfig(50);
z1 = (0, 0);
z2 = (2u, 3u);
z3 = (4u, 0);
z4 = .9[z1, z2];
z5 = .9[z1, z3];
draw z1 -- z2;
draw z1 -- z3;
draw z4 -- z5 dashed evenly;
dotlabel(btex $$ etex, z4);
dotlabel(btex $$ etex, z5);
endfig;

```

```

beginfig(51);
z1 = (0, 0);
z2 = (2u, 3u);
z3 = (4u, 0);
z4 = (.5u, 2.2u);

```

```

draw  $z_1$  --  $z_2$  dashed evenly;
draw  $z_1$  --  $z_3$ ;
draw  $z_4$  --  $z_3$  dashed evenly;
dotlabel(btex  $\$ \$$  etex,  $z_1$ );
dotlabel(btex  $\$ \$$  etex,  $z_3$ );
endfig;

beginfig(52);
 $z_1 = (0, 0)$ ;
 $z_2 = (u, 3u)$ ;
 $z_3 = (2u, 0)$ ;
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw_marked( $z_1$  --  $z_2$ , 1);
draw_marked( $z_2$  --  $z_3$ , 1);
mark_ang( $z_3$ ,  $z_1$ ,  $z_2$ ,  $.5u$ );
mark_ang( $z_2$ ,  $z_3$ ,  $z_1$ ,  $.5u$ );
endfig;

beginfig(53);
 $z_1 = (0, 0)$ ;
 $z_2 = (1.5u, 3u)$ ;
 $z_3 = (5u, 0)$ ;
 $z_4 = (1.5u, -3u)$ ;
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw  $z_1$  --  $z_4$  --  $z_3$ ;
draw  $z_2$  --  $z_4$  dashed evenly;
draw_marked( $z_1$  --  $z_2$ , 1);
markcommon( $z_1$ ,  $z_3$ );
draw_marked( $z_1$  --  $z_4$ , 1);
draw_marked( $z_2$  --  $z_3$ , 2);
draw_marked( $z_4$  --  $z_3$ , 2);
mark_ang( $z_1$ ,  $z_2$ ,  $z_4$ ,  $.7u$ );
mark_ang( $z_2$ ,  $z_4$ ,  $z_1$ ,  $.7u$ );
mark_angtwice( $z_4$ ,  $z_2$ ,  $z_3$ ,  $.5u$ );
mark_angtwice( $z_3$ ,  $z_4$ ,  $z_2$ ,  $.5u$ );
label ulft(btex  $\$A\$$  etex,  $z_1$ );
label top(btex  $\$B\$$  etex,  $z_2$ );
label urt(btex  $\$C\$$  etex,  $z_3$ );
label lft(btex  $\$ \alpha_1 \$$  etex,  $z_1$ );
label bot(btex  $\$ \alpha_1 \$$  etex,  $z_4$ );
label lrt(btex  $\$ \alpha_1 \$$  etex,  $z_3$ );
endfig;

beginfig(54);
 $z_1 = (0, 0)$ ;
 $z_2 = z_1$  shifted ( $u, 2u$ );
 $z_4 = (4u, 0)$ ;
 $z_3 = z_4$  shifted ( $u, 2u$ );
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw  $z_2$  --  $z_4$ ;
draw  $z_1$  --  $z_3$ ;
 $z_5 = \text{whatever}[z_2, z_4] = \text{whatever}[z_1, z_3]$ ;
draw_marked( $z_2$  --  $z_5$ , 1);
draw_marked( $z_5$  --  $z_4$ , 1);

```

```

draw_marked(z1 -- z5, 2);
draw_marked(z5 -- z3, 2);
mark_ang(z2, z5, z1, .5u);
mark_ang(z4, z5, z3, .5u);
label lft(btex  $A$  etex, z1);
label lft(btex  $B$  etex, z2);
label rt(btex  $C$  etex, z3);
label rt(btex  $D$  etex, z4);
label top(btex  $O$  etex, z5);
endfig;

beginfig(55);
z1 = (0, 0);
z2 = z1 shifted (-u, 2u);
z4 = (4u, 0);
z3 = z4 shifted (-u, 2u);
z5 = whatever[z2, z4] = whatever[z1, z3];
draw z1 -- z2 dashed evenly;
draw z3 -- z4;
draw z2 -- z4;
draw z1 -- z3;
draw_marked(z2 -- z5, 2);
draw_marked(z5 -- z4, 2);
draw_marked(z1 -- z5, 1);
draw_marked(z5 -- z3, 1);
mark_ang(z2, z5, z1, .5u);
mark_ang(z4, z5, z3, .5u);
label lft(btex  $D$  etex, z1);
label lft(btex  $E$  etex, z2);
label rt(btex  $B$  etex, z3);
label rt(btex  $S$  etex, .5[z3, z4]);
label rt(btex  $C$  etex, z4);
label bot(btex  $A$  etex, z5);
endfig;

beginfig(56);
z1 = (0, 0);
z2 = z1 shifted (-u, 2u);
z4 = (4u, 0);
z3 = z4 shifted (-u, 2u);
z5 = whatever[z2, z4] = whatever[z1, z3];
draw z2 -- z3 -- z4 dashed evenly;
draw z1 -- z2 -- z4 -- cycle;
draw_marked(z2 -- z5, 2);
draw_marked(z5 -- z4, 2);
draw_marked(z1 -- z5, 1);
draw_marked(z5 -- z3, 1);
label lft(btex  $A$  etex, z1);
label lft(btex  $C$  etex, z2);
dotlabel rt(btex  $N$  etex, z3);
label bot(btex  $S$  etex, .5[z1, z4]);
label lft(btex  $A$  etex, .5[z1, z2]);
label rt(btex  $B$  etex, z4);
label bot(btex  $M$  etex, z5);

```



```

endfig;

beginfig(57);
 $z_1 = (0, 0);$ 
 $z_2 = (u, 2u);$ 
 $z_3 = (4u, .3u);$ 
 $z_4 = .5[z_2, z_3];$ 
path  $p, r, rr;$ 
 $p = z_1 -- z_2 -- z_3 -- cycle;$ 
 $r = z_1 -- z_2 -- z_4 -- cycle;$ 
 $tr(r, 45);$ 
draw  $p;$ 
draw  $r;$ 
picture  $fir;$ 
 $fir = currentpicture;$ 
 $rr = r$  shifted  $(0, -4u);$ 
draw  $fir$  shifted  $(0, -4u);$ 
draw  $fir;$ 
label  $lft(\text{btex } \$A\$ \text{etex}, z_1);$ 
label  $lft(\text{btex } \$B\$ \text{etex}, z_2);$ 
label  $wrt(\text{btex } \$M\$ \text{etex}, z_4);$ 
label  $rt(\text{btex } \$C\$ \text{etex}, z_3);$ 
label  $lft(\text{btex } \$A'\$ \text{etex}, z_1)$  shifted  $(0, -4u);$ 
label  $lft(\text{btex } \$B'\$ \text{etex}, z_2)$  shifted  $(0, -4u);$ 
label  $wrt(\text{btex } \$M'\$ \text{etex}, z_4)$  shifted  $(0, -4u);$ 
label  $rt(\text{btex } \$C'\$ \text{etex}, z_3)$  shifted  $(0, -4u);$ 
endfig;

beginfig(59);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (4u, 0);$ 
 $z_4 = .5[z_2, z_3];$ 
path  $p, q, r;$ 
 $p = z_1 -- z_2 -- z_3 -- cycle;$ 
draw  $p;$ 
 $q = z_1 -- z_4;$ 
draw  $q;$ 
 $r = z_1 -- z_2 -- z_4 -- cycle;$ 
draw  $p$  shifted  $(0, -4u);$ 
draw  $r$  shifted  $(0, -4u);$ 
label  $lft(\text{btex } \$A\$ \text{etex}, z_1);$ 
label  $lft(\text{btex } \$B\$ \text{etex}, z_2);$ 
label  $wrt(\text{btex } \$D\$ \text{etex}, z_4);$ 
label  $rt(\text{btex } \$C\$ \text{etex}, z_3);$ 
label  $lft(\text{btex } \$A'\$ \text{etex}, z_1)$  shifted  $(0, -4u);$ 
label  $lft(\text{btex } \$B'\$ \text{etex}, z_2)$  shifted  $(0, -4u);$ 
label  $wrt(\text{btex } \$D'\$ \text{etex}, z_4)$  shifted  $(0, -4u);$ 
label  $rt(\text{btex } \$C'\$ \text{etex}, z_3)$  shifted  $(0, -4u);$ 
endfig;

beginfig(60);
 $z_1 = (0, 0);$ 
 $z_2 = z_1$  shifted  $(u, 2u);$ 
 $z_4 = (4u, 0);$ 

```

```

 $z_3 = z_4$  shifted  $(u, 2u)$ ;
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw  $z_1$  --  $z_3$ ;
draw_marked( $z_1$  --  $z_2$ , 1);
draw_marked( $z_2$  --  $z_3$ , 2);
draw_marked( $z_3$  --  $z_4$ , 1);
draw_marked( $z_4$  --  $z_1$ , 2);
label lft(btex  $\$A\$$  etex,  $z_1$ );
label lft(btex  $\$B\$$  etex,  $z_2$ );
label rt(btex  $\$C\$$  etex,  $z_3$ );
label rt(btex  $\$D\$$  etex,  $z_4$ );
endfig;

```

```

beginfig(61);
 $z_1 = (0, 0)$ ;
 $z_2 = (2u, 2u)$ ;
 $z_3 = (4u, 0)$ ;
 $z_{11} = z_1$  shifted  $(-4u, 0)$ ;
 $z_{12} = z_1$  shifted  $(0, -4u)$ ;
 $z_{21} = z_2$  shifted  $(.1u, .5u)$ ;
 $z_{22} = z_2$  shifted  $(.5u, .1u)$ ;
 $z_{23} = z_2$  shifted  $(-.5u, .1u)$ ;
 $z_{24} = z_2$  shifted  $(-.1u, .5u)$ ;
 $z_{31} = z_3$  shifted  $(0, -4u)$ ;
 $z_{32} = z_3$  shifted  $(.4u, 0)$ ;
 $z_{41} = z_1$  shifted  $(-.2828u, -.2828u)$ ;
 $z_{42} = z_1$  shifted  $(-.2828u, .2828u)$ ;
 $z_{51} = z_3$  shifted  $(.2828u, -.2828u)$ ;
 $z_{52} = z_3$  shifted  $(.2828u, .2828u)$ ;
dotlabel(btex  $\$ \$$  etex,  $z_1$ );
dotlabel(btex  $\$ \$$  etex,  $z_2$ );
dotlabel(btex  $\$ \$$  etex,  $z_3$ );
draw  $z_{11}$  --  $z_{21}$  --  $z_{22}$  --  $z_{12}$  -- cycle;
draw  $z_{23}$  --  $z_{24}$  --  $z_{32}$  --  $z_{31}$  -- cycle;
draw  $z_{41}$  --  $z_{42}$  --  $z_{52}$  --  $z_{51}$  -- cycle;
endfig;

```

```

beginfig(62);
 $z_1 = (0, 0)$ ;
 $z_2 = (-u, 1.5u)$ ;
 $z_3 = (0, 4u)$ ;
 $z_4 = (3u, 1.5u)$ ;
 $z_5 = (-2u, 1.5u)$ ;
 $z_6 = (4u, 1.5u)$ ;
dotlabel(btex  $\$ \$$  etex,  $z_1$ );
dotlabel(btex  $\$ \$$  etex,  $z_2$ );
dotlabel(btex  $\$ \$$  etex,  $z_3$ );
dotlabel(btex  $\$ \$$  etex,  $z_4$ );
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
drawarrow  $z_2$  shifted  $(-.2u, 0)$  ..  $z_5$ ;
drawarrow  $z_4$  shifted  $(.2u, 0)$  ..  $z_6$ ;
draw( $z_1$  shifted  $(0, .5u)$  --  $z_2$  shifted  $(-.5u, 0)$  --  $z_3$  shifted  $(0, -.5u)$  --  $z_4$  shifted  $(0.5u, 0)$  -- cycle) shifted
 $(0, -4u)$ ;
dotlabel(btex  $\$ \$$  etex,  $z_1$  shifted  $(0, -3.5u)$ );

```

```

dotlabel(btex $$ etex, z2 shifted (-.5u, -4u));
dotlabel(btex $$ etex, z3 shifted (0, -4.5u));
dotlabel(btex $$ etex, z4 shifted (0.5u, -4u));
endfig;

```

```

beginfig(63);
z0 = (0, 0);
z1 = (u, 1.5u);
z2 = (2u, 0);
path p;
path q;
p = z0 -- z1 -- z2 -- cycle;
draw p;
q = p scaled 2 shifted (3u, 0);
draw q;
endfig;

```

```

beginfig(64);
z1 = (0, 0);
z2 = z1 shifted (u, 2u);
z4 = (4u, 0);
z3 = z4 shifted (u, 2u);
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z1 -- z3;
mark_ang(z4, z1, z3, .4u);
mark_angtwice(z3, z1, z2, .5u);
mark_ang(z2, z3, z1, .4u);
mark_angtwice(z1, z3, z4, .5u);
label lft(btex $$ etex, z1);
label lft(btex $$ etex, z2);
label rt(btex $$ etex, z3);
label rt(btex $$ etex, z4);
endfig;

```

```

beginfig(65);
z1 = (0, 0);
z2 = (u, 3u);
z3 = (2u, 0);
z4 = z1 shifted (2.5u, -4u);
path p, q;
p = z1 -- z2 -- z3 -- cycle;
q = p shifted (2.5u, -4u) rotatedaround(z4, 90);
draw p;
draw q;
mark_ang(z3, z1, z2, angle_radius);
mark_ang(z2, z3, z1, angle_radius);
draw_marked(z1 -- z2, 1);
draw_marked(z3 -- z2, 1);
endfig;

```

```

beginfig(67);
z1 = (0, 0);
z3 = (2.5u, 0);
z4 = .5[z1, z3];
z2 = z4 shifted (0, 3u);

```

```

path  $p$ ;
 $p = z_1 -- z_2 -- z_3 -- cycle$ ;
draw  $p$ ;
draw  $z_2 -- z_4$ ;
 $draw\_marked(z_1 -- z_2, 1)$ ;
 $draw\_marked(z_3 -- z_2, 1)$ ;
 $draw\_marked(z_1 -- z_4, 2)$ ;
 $draw\_marked(z_4 -- z_3, 2)$ ;
label  $top$ (btex  $\$A\$$  etex,  $z_2$ );
label  $lft$ (btex  $\$B\$$  etex,  $z_1$ );
label  $rt$ (btex  $\$C\$$  etex,  $z_3$ );
label  $bot$ (btex  $\$M\$$  etex,  $z_4$ );
endfig;

beginfig(68);
 $z_1 = (0, 0)$ ;
 $z_3 = (2.5u, 0)$ ;
 $z_4 = .5[z_1, z_3]$ ;
 $z_2 = z_4$  shifted  $(0, 3u)$ ;
path  $p$ ;
 $p = z_1 -- z_2 -- z_3 -- cycle$ ;
draw  $p$ ;
draw  $z_2 -- z_4$ ;
 $draw\_marked(z_1 -- z_2, 1)$ ;
 $draw\_marked(z_3 -- z_2, 1)$ ;
 $mark\_ang(z_1, z_2, z_4, angle\_radius)$ ;
 $mark\_ang(z_4, z_2, z_3, 10pt)$ ;
label  $top$ (btex  $\$A\$$  etex,  $z_2$ );
label  $lft$ (btex  $\$B\$$  etex,  $z_1$ );
label  $rt$ (btex  $\$C\$$  etex,  $z_3$ );
label  $bot$ (btex  $\$M\$$  etex,  $z_4$ );
endfig;

beginfig(69);
 $z_1 = (0, 0)$ ;
 $z_3 = (2.5u, 0)$ ;
 $z_4 = .5[z_1, z_3]$ ;
 $z_2 = z_4$  shifted  $(0, 3u)$ ;
path  $p$ ;
 $p = z_1 -- z_2 -- z_3 -- cycle$ ;
draw  $p$ ;
draw  $z_2 -- z_4$ ;
 $draw\_marked(z_1 -- z_2, 1)$ ;
 $draw\_marked(z_3 -- z_2, 1)$ ;
 $mark\_rt\_angle(z_2, z_4, z_1)$ ;
 $mark\_rt\_angle(z_3, z_4, z_2)$ ;
label  $top$ (btex  $\$A\$$  etex,  $z_2$ );
label  $lft$ (btex  $\$B\$$  etex,  $z_1$ );
label  $rt$ (btex  $\$C\$$  etex,  $z_3$ );
label  $bot$ (btex  $\$M\$$  etex,  $z_4$ );
endfig;

beginfig(70);
 $z_1 = (0, 0)$ ;
 $z_3 = (2.5u, 0)$ ;

```

```

z4 = .5[z1, z3];
z2 = z4 shifted (0, 3u);
z5 = z4 shifted (0, -3u);
path p;
p = z1 -- z2 -- z3 -- cycle;
draw p;
draw z2 -- z4;
draw z4 -- z5;
draw z1 -- z5 dashed evenly;
draw_marked(z1 -- z4, 1);
draw_marked(z4 -- z3, 1);
draw_marked(z2 -- z4, 2);
draw_marked(z4 -- z5, 2);
mark_ang(z1, z2, z4, angle_radius);
mark_ang(z4, z2, z3, 10pt);
label top(btex  $\$A\$$  etex, z2);
label lft(btex  $\$B\$$  etex, z1);

label rt(btex  $\$C\$$  etex, z3);
label ulft(btex  $\$M\$$  etex, z4);
label bot(btex  $\$N\$$  etex, z5);
endfig;

```

```

beginfig(73);
z1 = (0, 0);
z3 = (2.5u, 0);
z4 = .5[z1, z3];
z2 = z4 shifted (0, 3u);
z5 = z4 shifted (0, -3u);
path p;
p = z1 -- z2 -- z3 -- cycle;
draw p;
draw z2 -- z4 dashed evenly;
draw_marked(z1 -- z2, 1);
draw_marked(z2 -- z3, 1);
label top(btex  $\$X\$$  etex, z2);
label lft(btex  $\$A\$$  etex, z1);
label rt(btex  $\$B\$$  etex, z3);
label bot(btex  $\$M\$$  etex, z4);
endfig;

```

```

beginfig(75);
z1 = (0, 0);
z3 = (4u, 0);
z2 = (1.5u, 1.5u);
z4 = (1.5u, -1.5u);
path p, q, r;
p = z1 -- z2 -- z3 -- z4 -- cycle;
draw p;
draw z1 -- z3;
draw z2 -- z4;
draw_marked(z1 -- z2, 1);
draw_marked(z1 -- z4, 1);
draw_marked(z2 -- z3, 2);
draw_marked(z3 -- z4, 2);

```

```

endfig;

beginfig(76);
 $z_1 = (0, 0);$ 
path  $a;$ 
 $a = \text{fullcircle scaled } 4u;$ 
 $z_2 = \text{point 1 of } a;$ 
 $z_3 = \text{point 7 of } a;$ 
draw  $a;$ 
draw  $z_1 -- z_2;$ 
draw  $z_1 -- z_3;$ 
pickup pencircle scaled } 0.2u;
drawdot  $z_1;$ 
drawdot  $z_2;$ 
drawdot  $z_3;$ 
endfig;

beginfig(77);
 $z_1 = (0, 0);$ 
path  $a;$ 
 $a = \text{fullcircle scaled } 4u;$ 
 $z_2 = \text{point 1 of } a;$ 
 $z_3 = \text{point 7 of } a;$ 
draw  $a;$ 
draw  $z_1 -- z_2;$ 
draw  $z_1 -- z_3;$ 
draw  $z_2 -- z_3;$ 
pickup pencircle scaled } 0.2u;
drawdot  $z_1;$ 
drawdot  $z_2;$ 
drawdot  $z_3;$ 
endfig;

beginfig(78);
 $z_1 = (0, 0);$ 
 $z_4 = (1.2u, -u);$ 
path  $a;$ 
 $a = \text{fullcircle scaled } 4u;$ 
 $z_2 = (2.4u, 0);$ 
 $z_3 = (1.7u, -2.3u);$ 
draw  $a;$ 
draw  $a$  shifted  $(2.4u, 0);$ 
draw  $a$  shifted  $(1.7u, -2.3u);$ 
draw  $z_1 -- z_4$  dashed evenly;
draw  $z_2 -- z_4$  dashed evenly;
draw  $z_3 -- z_4$  dashed evenly;
pickup pencircle scaled } 0.2u;
drawdot  $z_1;$ 
drawdot  $z_2;$ 
drawdot  $z_3;$ 
drawdot  $z_4;$ 
endfig;

beginfig(79);
 $z_1 = (0, 0);$ 

```

```

z2 = (1.5u, 0);
z3 = (3.5u, 0);
z4 = (6u, 0);
path a, b;
a = fullcircle scaled 3u;
b = fullcircle scaled 5u shifted z4; ;
draw a;
draw b;
drawarrow z1 .. z2;
drawarrow z4 .. z3;
label top(btex $3$ etex, .5[z1, z2]);
label top(btex $5$ etex, .5[z3, z4]);
endfig;

beginfig(80);
z1 = (0, 0);
z2 = (.5u, 0);
z3 = (-.5u, -1.4u);
z4 = (2u, 2u);
path a, b;
a = fullcircle scaled 3u;
b = fullcircle scaled 5u shifted (.5u, 0);
draw a;
draw b;
draw z1 .. z2;
drawarrow z1 .. z3;
drawarrow z2 .. z4;
label top(btex $1$ etex, .5[z1, z2]);
label ulft(btex $3$ etex, .5[z1, z3]);
label top(btex $5$ etex, .5[z2, z4]);
endfig;

beginfig(81);
z1 = (0, 0);
path a;
a = fullcircle scaled 4u;
z2 = (3u, 0);
draw a;
draw a shifted z2;
pickup pencircle scaled 0.2u;
drawdot z1;
drawdot z2;
picture q;
q = currentpicture;
draw q shifted (0, 6u);
endfig;

beginfig(83);
z1 = (0, 0);
path a;
a = fullcircle scaled 4u;
z2 = point 2 of a;
z3 = point 3.6 of a;
draw a;
draw(-2u, 0) -- (2u, 0);

```

```

draw  $z_2$  --  $z_3$ ;
pickup pencircle scaled  $0.2u$ ;
drawdot  $z_1$ ;
drawdot  $z_2$ ;
drawdot  $z_3$ ;

beginfig(84);
 $z_1 = (0, 0)$ ;
path  $a$ ;
 $a = \text{fullcircle}$  scaled  $4u$ ;
 $z_2 = \text{point } 1 \text{ of } a$ ;
 $z_3 = \text{point } 4 \text{ of } a$ ;
draw  $a$ ;
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
pickup pencircle scaled  $0.2u$ ;
drawdot  $z_1$ ;
drawdot  $z_2$ ;
drawdot  $z_3$ ;
endfig;
endfig;

beginfig(85);
 $z_1 = (0, 0)$ ;
path  $a$ ;
 $a = \text{fullcircle}$  scaled  $4u$ ;
 $z_2 = \text{point } 1 \text{ of } a$ ;
 $z_3 = \text{point } 4 \text{ of } a$ ;
 $z_4 = .5[z_2, z_3]$ ;
draw  $a$ ;
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw  $z_1$  --  $z_4$ ;
 $\text{draw\_marked}(z_2$  --  $z_4, 1)$ ;
 $\text{draw\_marked}(z_3$  --  $z_4, 1)$ ;
 $\text{draw\_marked}(z_1$  --  $z_2, 2)$ ;
 $\text{draw\_marked}(z_1$  --  $z_3, 2)$ ;
pickup pencircle scaled  $0.2u$ ;
drawdot  $z_1$ ;
drawdot  $z_2$ ;
drawdot  $z_3$ ;
drawdot  $z_4$ ;
endfig;

beginfig(86);
 $z_1 = (0, 0)$ ;
 $z_2 = (-2u, 0)$ ;
 $z_3 = (2u, 0)$ ;
draw  $(-2.5u, 0)$  --  $(2.5u, 0)$ ;
draw  $(z_2$  --  $z_3$  scaled  $.2$ ) shifted  $(.5u, 2u)$ ;
label bot(btex  $\text{\$A\$}$  etex,  $z_1$ );
label bot(btex  $\text{\$B\$}$  etex,  $z_2$ );
label bot(btex  $\text{\$C\$}$  etex,  $z_3$ );
pickup pencircle scaled  $0.2u$ ;
drawdot  $z_1$ ;
drawdot  $z_2$ ;
drawdot  $z_3$ ;

```



```

draw z2 shifted (.5u, 2u);
draw z3 shifted (-u, 2u);
endfig;

beginfig(87);
z1 = (0, 0);
z2 = (3u, .5u);
z3 = (2.2u, 2.3u);
draw z1 -- z2 -- z3 -- cycle;
label llft(btex  $\$A\$$  etex, z1);
label lrt(btex  $\$B\$$  etex, z2);
label urt(btex  $\$C\$$  etex, z3);
endfig;

beginfig(88);
z1 = (-u, 2u);
z2 = (2u, -u);
path a, b, c, d, e;
numeric rad;
rad = 3u;
a = fullcircle scaled 2rad shifted z1;
b = fullcircle scaled 2rad shifted z2;
z10 = point 0.2 of a;
z16 = point 5.8 of a;
z17 = point 7 of a;
z22 = point 1.8 of b;
z23 = point 3 of b;
z24 = point 4.2 of b;
c = z16 .. z17 .. z10;
d = z22 .. z23 .. z24;
e = subpath(6, 7) of a;
z3 = a intersectionpoint b;
z4 = e intersectionpoint b;
draw c;
draw d;
draw z1 -- z2;
label llft(btex  $\$A'\$$  etex, z1);
label lrt(btex  $\$B'\$$  etex, z2);
pickup pencircle scaled 0.2u;
drawdot z1;
drawdot z2;
drawdot z3;
drawdot z4;
endfig;

beginfig(89);
z0 = (0, 0);
z11 = (2.5u, 2u);
z12 = (3u, 0);
z4 = (0, -2u);
path a, b;
a = z0 -- z11;
z1 = point 0.7 of a;
z2 = (2.6u, 0);
b = z0 -- z1 -- z2 -- cycle;

```

```



```

```

draw a;
draw z0 -- z12;
z11 = z12 zscaled (co, si);
z4 = z12 rotated (.5 * angle(co, si));
b = z0 -- z4;
draw b dashed evenly;
z14 = point 1.7 of b;
label top(btex  $X$  etex, z14);
endfig;

beginfig(91);
z1 = (-u, 0);
z2 = (2u, 0);
path a, b, c, d, e, f;
numeric rad;
rad = 2u;
a = fullcircle scaled 2rad shifted z1;
b = fullcircle scaled 2rad shifted z2;
z10 = point 0 of a;
z11 = point 1.2 of a;
z17 = point 6.8 of a;
z23 = point 2.8 of b;
z24 = point 4 of b;
z25 = point 5.2 of b;
c = z17 .. z10 .. z11;
d = z23 .. z24 .. z25;
e = subpath(7, 8) of a;
z3 = a intersectionpoint b;
z4 = e intersectionpoint b;
draw c;
draw d;
f = (z3 -- z4) yscaled 1.2;
draw f dashed evenly;
draw z1 -- z2;
label lft(btex  $A$  etex, .5[z1, z2] shifted (-.3u, 0));
pickup pencircle scaled 0.2u;
drawdot z1;
drawdot z2;
drawdot z3;
drawdot z4;
endfig;

beginfig(92);
z1 = (-u, 0);
z2 = (2u, 0);
path a, b, c, d, e, f;
numeric rad;
rad = 1.8u;
a = fullcircle scaled 2rad shifted z1;
b = fullcircle scaled 2rad shifted z2;
z10 = point 0 of a;
z11 = point 1.2 of a;
z17 = point 6.8 of a;
z23 = point 2.8 of b;

```

```

z24 = point 4 of b;
z25 = point 5.2 of b;
c = z17 .. z10 .. z11;
d = z23 .. z24 .. z25;
e = subpath(7, 8) of a;
z3 = a intersectionpoint b;
z4 = e intersectionpoint b;
draw c dashed evenly;
draw d;
z31 = z3 shifted (1.3u, 0);
z41 = z3 shifted (1.3u, 0);
f = z3 .. z31 .. z41 .. z4 .. cycle;
z5 = .5[z4, z31];
draw f;
draw(-.7u, 0) -- (3u, 0);
z6 = (2.5u, 0);
label lft(btex  $\$A\$$  etex, z3);
label bot(btex  $\$1\$$  etex, z6);
pickup pencircle scaled 0.2u;
drawdot z5;
drawdot z6;
drawdot z3;
drawdot z4;
endfig;

beginfig(93);
z1 = (0, 0);
z2 = (2.5u, 2u);
draw z1 -- z2;
draw(z1 -- z2) shifted (0, u);
endfig;

beginfig(94);
z0 = (0, 2u);
z1 = (2.5u, 4u);
draw z0 -- z1;
draw(z0 -- z1) shifted (0, u) dashed evenly;
z2 = (-.5u, 0);
z3 = (3u, 0);
z4 = (0, 1.2u);
z5 = (3.5u, 1.2u);
z6 = (.7u, -0.5u);
z7 = (2.3u, 2.2u);
z8 = whatever[z2, z3] = whatever[z6, z7];
z9 = whatever[z4, z5] = whatever[z6, z7];
draw z2 -- z3;
draw z4 -- z5;
draw z6 -- z7;
mark_ang(z3, z8, z9, angle_radius);
mark_ang(z5, z9, z7, angle_radius);
pickup pencircle scaled 0.2u;
drawdot .5[z0, z1] shifted (0, u);
endfig;

beginfig(96);

```

```

z_0 = (0, 3u);
z_1 = (2.5u, 3u);
draw z_0 -- z_1;
draw (z_0 -- z_1) shifted (0, -u);
draw (z_0 -- z_1) shifted (0, -2u);
z_2 = z_1 shifted (0, -u);
z_3 = (4u, 2.5u);
z_4 = z_1 shifted (0, -2u); ;
draw z_1 -- z_3 dashed evenly;
draw z_2 -- z_3 dashed evenly;
label ulft(btex $m$ etex, z_0);
label ulft(btex $m$ etex, z_0 shifted (0, -u));
label urt(btex $X?$ etex, z_3);
label lrt(btex $l$ etex, z_1 shifted (0, -2u));
pickup pencircle scaled 0.2u;
drawdot z_3;
endfig;

```

```

beginfig(97);
z_2 = (-.5u, 0);
z_3 = (3u, 0);
z_4 = (0, 1.2u);
z_5 = (3.5u, 1.2u);
z_0 = (.7u, 2.4u);
z_1 = (4u, 2.4u);
z_6 = (.7u, -0.5u);
z_7 = (2.5u, 3.8u);
z_8 = whatever[z_2, z_3] = whatever[z_6, z_7];
z_9 = whatever[z_4, z_5] = whatever[z_6, z_7];
z_10 = whatever[z_0, z_1] = whatever[z_6, z_7];
draw z_0 -- z_1;
draw z_2 -- z_3;
draw z_4 -- z_5;
draw z_6 -- z_7;
mark_ang(z_3, z_8, z_9, angle_radius);
mark_ang(z_5, z_9, z_7, angle_radius);
mark_ang(z_1, z_10, z_7, angle_radius);
endfig;

```

```

beginfig(98);
z_0 = (0, 0);
z_1 = (2u, 0);
z_2 = (0, 1.2u);
z_3 = (2u, 1.2u);
z_4 = (u, -.5u);
z_5 = (u, 1.7u);
z_6 = wharever[z_0, z_1] = whatever[z_4, z_5];
z_7 = whatever[z_2, z_3] = whatever[z_4, z_5];
draw z_0 -- z_1;
draw z_2 -- z_3;
draw z_4 -- z_5;
mark_rt_angle(z_1, z_6, z_7);
mark_rt_angle(z_3, z_7, z_5);
mark_rt_angle(z_2, z_7, z_6);

```

```

mark_rt_angle(z0, z6, z4);
endfig;

beginfig(99);
z2 = (-.5u, 0);
z3 = (3u, 0);
z4 = (0, 1.2u);
z5 = (3.5u, 1.2u);
z6 = (.7u, -0.5u);
z7 = (2u, 2.2u);
z8 = whatever[z2, z3] = whatever[z6, z7];
z9 = whatever[z4, z5] = whatever[z6, z7];
draw z2 -- z3;
draw z4 -- z5;
draw z6 -- z7;
endfig;

beginfig(100);
z2 = (-.5u, 0);
z3 = (3u, 0);
z4 = (0, 1.2u);
z5 = (3.5u, 1.2u);
z6 = (.7u, -0.5u);
z7 = (2u, 2.2u);
z8 = whatever[z2, z3] = whatever[z6, z7];
z9 = whatever[z4, z5] = whatever[z6, z7];
draw z2 -- z3;
draw z4 -- z5;
draw z6 -- z7;
mark_ang(z3, z8, z9, angle_radius);
mark_ang(z4, z9, z8, angle_radius);
endfig;

beginfig(101);
z2 = (-.5u, 0);
z3 = (3u, 0);
z4 = (0, 1.2u);
z5 = (3.5u, 1.2u);
z6 = (.7u, -0.5u);
z7 = (2u, 2.2u);
z8 = whatever[z2, z3] = whatever[z6, z7];
z9 = whatever[z4, z5] = whatever[z6, z7];
draw z2 -- z3;
draw z4 -- z5;
draw z6 -- z7;
mark_ang(z3, z8, z9, 4pt);
mark_angtwice(z8, z9, z5, 4pt);
endfig;

beginfig(102);
z1 = (0, 2u);
z2 = (3u, 3.5u);
z3 = .5[z1, z2];
z4 = z2 rotatedaround(z3, 90);
draw z1 -- z2;

```

```

drawarrow z4 -- z3 dashed evenly;
path p, q;
p = (z1 -- z2) rotated -40 shifted (-u, 0);
q = (z3 -- z4) rotated -40 shifted (-u, 0);
draw p;
drawarrow q dashed evenly;
endfig;

beginfig(104);
z1 = (0, 0);
z2 = (u, 2.5u);
z3 = (3u, 2.5u);
z4 = (4u, 0);
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z1 -- z3;
mark_ang(z4, z1, z3, angle_radius);
mark_ang(z2, z3, z1, angle_radius);
label llft(btex  $\$A\$$  etex, z1);
label ulft(btex  $\$B\$$  etex, z2);
label urt(btex  $\$C\$$  etex, z3);
label lrt(btex  $\$D\$$  etex, z4);
endfig;

beginfig(106);
z1 = (0, 2u);
z2 = (3u, 2u);
z3 = (u, 3u);
z4 = (u, u);
draw z1 -- z2;
draw z3 -- z4;
z11 = z1 shifted (1.5u, -2u);
z22 = z2 shifted (1.5u, -2u);
z33 = (z3 yscaled 1.8) shifted (1.5u, -2.5u);
z44 = (z4 yscaled 1.7) shifted (1.5u, -2.5u);
z5 = whatever[z1, z2] = whatever[z3, z4];
z6 = whatever[z1, z2] = whatever[z33, z44];
z7 = whatever[z11, z22] = whatever[z33, z44];
draw z11 -- z22;
draw z33 -- z44;
mark_rt_angle(z2, z5, z3);
mark_rt_angle(z2, z6, z33);
mark_rt_angle(z22, z7, z33);
label bot(btex  $\$12\$$  etex, z1);
label bot(btex  $\$11\$$  etex, z11);
label urt(btex  $\$m2\$$  etex, z3);
label urt(btex  $\$m1\$$  etex, z33);
endfig;

beginfig(107);
z1 = (u, 2.7u);
z2 = (0, 0);
z3 = (2u, 0);
z11 = z1 shifted (.7u, -1.5u);
z22 = z2 shifted (.7u, -1.5u);

```

```

z33 = z3 shifted (.7u, -1.5u);
draw z1 -- z2 -- z3;
draw z11 -- z22 -- z33;
mark_ang(z3, z2, z1, angle_radius);
mark_ang(z33, z22, z11, angle_radius);
endfig;

beginfig(108);
z1 = (u, 2.7u);
z2 = (0, 0);
z3 = (2u, 0);
z11 = z1 shifted (.7u, -1.5u);
z22 = z2 shifted (.7u, -1.5u);
z33 = z3 shifted (.7u, -1.5u);
z4 = whatever[z2, z3] = whatever[z11, z22];
draw z1 -- z2 -- z3;
draw z11 -- z22 -- z33;
mark_ang(z3, z2, z1, angle_radius);
mark_ang(z33, z22, z11, angle_radius);
mark_ang(z3, z4, z11, angle_radius);
endfig;

beginfig(109);
z1 = (0, 0);
z2 = (3u, 0);
z4 = z1 shifted (0, 1.5u);
z5 = z2 shifted (0, 1.5u);
z3 = .4[z4, z5];
draw z1 -- z2 -- z3 -- cycle;
draw z4 -- z5;
mark_ang(z2, z1, z3, angle_radius);
mark_ang(z4, z3, z1, angle_radius);
mark_angtwice(z3, z2, z1, angle_radius);
mark_angtwice(z2, z3, z5, angle_radius);
label lft(btex  $\$A\$$  etex, z1);
label top(btex  $\$B\$$  etex, z3);
label lrt(btex  $\$C\$$  etex, z2);
endfig;

beginfig(110);
z1 = (0, 0);
z2 = (3u, 0);
z3 = z2 rotated 60;
label wrt(btex  $\$60\$$  etex, z1 shifted (.2u, 0));
label bot(btex  $\$60\$$  etex, z3 shifted (0, -.4u));
label ulft(btex  $\$60\$$  etex, z2 shifted (-.2u, 0));
draw z1 -- z2 -- z3 -- cycle;
draw_marked(z1 -- z2, 1);
draw_marked(z1 -- z3, 1);
draw_marked(z3 -- z2, 1);
endfig;

beginfig(111);
z1 = (0, 0);
z2 = (u, 2.5u);

```



```

 $z_3 = (3u, 2.5u);$ 
 $z_4 = (4u, -1.2u);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw  $z_1$  --  $z_3$  dashed evenly;
endfig;

beginfig(112);
 $z_1 = (0, 0);$ 
 $z_2 = (-u, u);$ 
 $z_3 = (.5u, 2.5u);$ 
 $z_4 = (2u, 2u);$ 
 $z_5 = (2u, .5u);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  --  $z_5$  -- cycle;
draw  $z_1$  --  $z_3$  dashed evenly;
draw  $z_1$  --  $z_4$  dashed evenly;
endfig;

beginfig(113);
 $z_1 = (0, 0);$ 
 $z_2 = (3u, 0);$ 
 $z_3 = (u, 1.2u);$ 
 $z_4 = (-2u, 0);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw  $z_1$  --  $z_4$ ;
 $mark\_ang(z_1, z_3, z_2, 6pt);$ 
 $mark\_angtwice(z_3, z_2, z_1, angle\_radius);$ 
label lft(btex  $\$A\$$  etex,  $z_1$ );
label top(btex  $\$B\$$  etex,  $z_3$ );
label lrt(btex  $\$C\$$  etex,  $z_2$ );
endfig;

beginfig(114);
 $z_1 = (0, 0);$ 
 $z_2 = (2u, 0);$ 
 $z_3 = (3u, 2u);$ 
 $z_4 = .5[z_1, z_3];$ 
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw  $z_2$  --  $z_4$ ;
 $mark\_ang(z_1, z_4, z_2, 6pt);$ 
 $mark\_ang(z_4, z_2, z_1, 6pt);$ 
label lft(btex  $\$A\$$  etex,  $z_1$ );
label top(btex  $\$B\$$  etex,  $z_3$ );
label lrt(btex  $\$C\$$  etex,  $z_2$ );
label ulft(btex  $\$D\$$  etex,  $z_4$ );
endfig;

beginfig(115);
 $z_1 = (0, 0);$ 
 $z_2 = (u, 2u);$ 
 $z_3 = (3u, 0);$ 
 $z_{33} = (4u, 0);$ 
 $z_{11} = 1.4[z_2, z_1];$ 
 $z_{22} = 1.2[z_3, z_2];$ 
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw  $z_{11}$  --  $z_1$ ;

```

```

draw z22 -- z2;
draw z33 -- z3;
mark_ang(z11, z1, z3, 6pt);
mark_ang(z22, z2, z1, 6pt);
mark_ang(z33, z3, z2, 6pt);
endfig;

```

```

beginfig(116);
z1 = (0, u);
z2 = (u, 2u);
z3 = (3u, u);
z4 = (u, -.5u);
z11 = 1.4[z2, z1];
z22 = 1.4[z3, z2];
z33 = 1.4[z4, z3];
z44 = 1.4[z1, z4];
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z11 -- z1;
draw z22 -- z2;
draw z33 -- z3;
draw z44 -- z4;
mark_ang(z11, z1, z4, 6pt);
mark_ang(z22, z2, z1, 6pt);
mark_ang(z33, z3, z2, 6pt);
mark_ang(z44, z4, z3, 6pt);
endfig;

```

```

beginfig(117);
z1 = (0, u);
z2 = (u, 2u);
z3 = (3u, u);
z4 = (2u, -1.2u);
z5 = (.5u, -.5u);
z11 = 1.4[z2, z1];
z22 = 1.4[z3, z2];
z33 = 1.4[z4, z3];
z44 = 1.4[z5, z4];
z55 = 1.4[z1, z5];
draw z1 -- z2 -- z3 -- z4 -- z5 -- cycle;
draw z11 -- z1;
draw z22 -- z2;
draw z33 -- z3;
draw z44 -- z4;
draw z55 -- z5;
mark_ang(z11, z1, z5, 6pt);
mark_ang(z22, z2, z1, 6pt);
mark_ang(z33, z3, z2, 6pt);
mark_ang(z44, z4, z3, 6pt);
mark_ang(z55, z5, z4, 6pt);
endfig;

```

```

beginfig(118);
z1 = (u, 0);
z2 = (.5u, 2u);
z3 = (2u, 3u);

```

```

 $z_4 = (3.5u, 2u);$ 
 $z_5 = (3u, 0);$ 
draw  $z_1$  --  $z_3$  --  $z_5$  --  $z_2$  --  $z_4$  -- cycle;
mark_ang( $z_4, z_1, z_3, 6pt$ );
mark_ang( $z_5, z_2, z_4, 6pt$ );
mark_ang( $z_1, z_3, z_5, 6pt$ );
mark_ang( $z_2, z_4, z_1, 6pt$ );
mark_ang( $z_3, z_5, z_2, 6pt$ );
endfig;

beginfig(119);
 $z_1 = (0, 0);$ 
 $z_2 = (u, 2u);$ 
 $z_3 = (2u, 0);$ 
 $z_4 = .5[z_2, z_3];$ 
draw  $z_1$  --  $z_2$  --  $z_3$  -- cycle;
draw  $z_1$  --  $z_4$ ;
label lft(btex  $\$A\$$  etex,  $z_1$ );
label top(btex  $\$B\$$  etex,  $z_2$ );
label lrt(btex  $\$C\$$  etex,  $z_3$ );
label wrt(btex  $\$M\$$  etex,  $z_4$ );
endfig;

beginfig(120);
 $z_1 = (-u, .5u);$ 
 $z_2 = (1.5u, 3.5u);$ 
 $z_3 = (2.2u, 2u);$ 
 $z_4 = z_1$  shifted  $(3u, 0);$ 
 $z_5 = (z_2$  rotatedaround( $z_1, 90$ )) shifted  $(3u, 0);$ 
 $z_6 = (z_3$  rotatedaround( $z_1, 90$ )) shifted  $(3u, 0);$ 
 $z_{12} = \textit{whatever}[z_1, z_2] = \textit{whatever}[z_4, z_5];$ 
 $z_{21} = \textit{whatever}[z_1, z_2] = \textit{whatever}[z_4, z_6];$ 
 $z_{13} = \textit{whatever}[z_1, z_3] = \textit{whatever}[z_4, z_5];$ 
 $z_{31} = \textit{whatever}[z_1, z_3] = \textit{whatever}[z_4, z_6];$ 
path  $p;$ 
 $p = z_{12}$  --  $z_{21}$  --  $z_{31}$  --  $z_{13}$  -- cycle;
p, 45);
draw  $z_2$  --  $z_1$  --  $z_3$ ;
draw  $z_5$  --  $z_4$  --  $z_6$ ;
label lft(btex  $\$A\$$  etex,  $z_{12}$ );
label rt(btex  $\$B\$$  etex,  $z_{21}$ );
label rt(btex  $\$C\$$  etex,  $z_{31}$ );
label bot(btex  $\$D\$$  etex,  $z_{13}$ );
endfig;

beginfig(121);
 $z_1 = (-u, .5u);$ 
 $z_2 = (1.5u, 3.5u);$ 
 $z_3 = (2.2u, 2u);$ 
 $z_4 = (3u, 0);$ 
 $z_5 = (u, 4u);$ 
 $z_6 = (u, -.5u);$ 
 $z_{12} = \textit{whatever}[z_1, z_2] = \textit{whatever}[z_5, z_6];$ 
 $z_{13} = \textit{whatever}[z_1, z_3] = \textit{whatever}[z_5, z_6];$ 
 $z_{14} = \textit{whatever}[z_1, z_4] = \textit{whatever}[z_5, z_6];$ 

```

```

draw z2 -- z1 -- z3;
draw z1 -- z4;
draw z5 -- z6;
mark_ang(z3, z1, z2, 8pt);
mark_ang(z4, z1, z3, 6pt);
mark_ang(z2, z12, z5, 6pt);
mark_ang(z3, z13, z5, 6pt);
mark_ang(z4, z14, z5, 6pt);
endfig;

beginfig(122);
z1 = (0, 0);
z2 = (3u, 0);
z3 = (1.5u, 2u);
z4 = .5[z1, z2];
draw z1 -- z2;
draw z4 -- z3;
mark_rt_angle(z2, z4, z3);
mark_rt_angle(z3, z4, z1);
draw_marked(z1 -- z3, 1);
draw_marked(z3 -- z2, 1);
label lft(btex  $A$  etex, z1);
label lrt(btex  $A'$  etex, z2);
label lft(btex  $C$  etex, z4);
label lrt(btex  $C'$  etex, z4);
label ulft(btex  $B$  etex, z3);
label urt(btex  $B'$  etex, z3);
endfig;

beginfig(123);
z1 = (0, 0);
z2 = (3u, 0);
z3 = (1.5u, 2u);
z4 = .5[z1, z2];
draw z1 -- z3 -- z2 -- cycle;
draw z4 -- z3;
label bot(btex  $x$  etex, .5[z1, z4]);
label bot(btex  $x$  etex, .5[z4, z2]);
label lft(btex  $2x$  etex, .5[z1, z3]);
label rt(btex  $2x$  etex, .5[z3, z2]);
endfig;

beginfig(124);
z1 = (0, 0);
z2 = (3u, 0);
z3 = (1.5u, 2u);
z4 = .5[z1, z2];
draw z1 -- z3 -- z2 -- cycle;
draw z4 -- z3;
mark_ang(z1, z3, z4, 6pt);
mark_ang(z4, z3, z2, 8pt);
label bot(btex  $30$  etex, z3 shifted (-.4u, -.8u));
label bot(btex  $30$  etex, z3 shifted (.4u, -.8u));
endfig;

```

```

beginfig(125);
 $z_1 = (0, 0);$ 
 $z_2 = (.5u, 2u);$ 
path  $p, q;$ 
pair  $d;$ 
 $p = ((z_1 -- z_2) \text{ scaled } 1.5);$ 
draw  $p$  shifted  $(-.1u, -.5u);$ 
draw  $p$  shifted  $(2.9u, -.5u);$ 
 $q = ((z_1 -- (3u, 0)) \text{ scaled } 1.5);$ 
draw  $q$  shifted  $(-.7u, 0);$ 
draw  $q$  shifted  $(-.2u, 2u);$ 
pickup pencircle scaled  $.14u;$ 
 $\text{parallelogram}(d, z_1, z_2)((3u, 0));$ 
endfig;

```

```

beginfig(126);
 $z_1 = (0, 0);$ 
 $z_2 = (.5u, 2u);$ 
path  $p, q;$ 
pair  $d;$ 
 $p = ((z_1 -- z_2) \text{ scaled } 1.5);$ 
draw  $p$  shifted  $(-.1u, -.5u);$ 
draw  $p$  shifted  $(2.9u, -.5u);$ 
 $q = ((z_1 -- (3u, 0)) \text{ scaled } 1.5);$ 
draw  $q$  shifted  $(-.7u, 0);$ 
draw  $q$  shifted  $(-.2u, 2u);$ 
pickup pencircle scaled  $.14u;$ 
 $\text{parallelogram}(d, z_1, z_2)((3u, 0));$ 
pickup pencircle scaled  $\text{penthtick};$ 
 $\text{mark\_ang}(d, z_1, z_2, \text{angle\_radius})$ 
endfig;

```

```

beginfig(133);
 $z_1 = (0, 0);$ 
 $z_2 = (2u, u);$ 
 $z_3 = (3u, 0);$ 
 $z_4 = z_1$  shifted  $(.5u, 2u);$ 
 $z_5 = z_2$  shifted  $(.5u, 2u);$ 
 $z_6 = z_3$  shifted  $(.5u, 2u);$ 
draw  $z_1 -- z_4 -- z_5 -- z_6 -- z_3 -- z_2 -- \text{cycle};$ 
draw  $z_2 -- z_5;$ 
draw  $z_1 -- z_3$  dashed  $\text{evenly};$ 
draw  $z_4 -- z_6$  dashed  $\text{evenly};$ 
label  $\text{llft}(\text{btex } \text{\$A\$ etex}, z_1);$ 
label  $\text{ulft}(\text{btex } \text{\$B\$ etex}, z_4);$ 
label  $\text{top}(\text{btex } \text{\$C\$ etex}, z_5);$ 
label  $\text{bot}(\text{btex } \text{\$D\$ etex}, z_2);$ 
label  $\text{urt}(\text{btex } \text{\$E\$ etex}, z_6);$ 
label  $\text{lrt}(\text{btex } \text{\$F\$ etex}, z_3);$ 
endfig;

```

```

beginfig(136);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (3u, 2u);$ 

```

```

 $z_4 = (3u, 0);$ 
path  $p, q;$ 
 $p = z_1 -- z_2 -- z_3 -- z_4 -- \text{cycle};$ 
draw  $p;$ 
draw  $p$  shifted  $(0, -3u);$ 
draw  $z_1 -- z_3;$ 
 $q = (z_2 -- z_4)$  shifted  $(0, -3u);$ 
draw  $q;$ 
endfig;

beginfig(137);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (3u, 0);$ 
 $z_4 = .5[z_2, z_3];$ 
path  $p;$ 
 $p = z_1 -- z_2 -- z_3 -- \text{cycle};$ 
draw  $p;$ 
draw  $z_1 -- z_4;$ 
 $\text{draw\_marked}(z_2 -- z_4, 1);$ 
 $\text{draw\_marked}(z_4 -- z_3, 1);$ 
endfig;

beginfig(138);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (3u, 0);$ 
 $z_4 = .5[z_2, z_3];$ 
 $z_5 = (3u, 2u);$ 
path  $p;$ 
 $p = z_1 -- z_2 -- z_3 -- \text{cycle};$ 
draw  $p;$ 
draw  $z_1 -- z_4;$ 
draw  $z_1 -- z_5;$ 
draw  $z_2 -- z_5 -- z_3$  dashed evenly;
 $\text{draw\_marked}(z_2 -- z_4, 1);$ 
 $\text{draw\_marked}(z_4 -- z_3, 1);$ 
 $\text{draw\_marked}(z_1 -- z_4, 2);$ 
 $\text{draw\_marked}(z_4 -- z_5, 2);$ 
endfig;

beginfig(139);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 3u);$ 
 $z_3 = (2u, 0);$ 
 $z_4 = .5[z_2, z_3];$ 
path  $p;$ 
 $p = z_1 -- z_2 -- z_3 -- \text{cycle};$ 
draw  $p;$ 
drawarrow  $(1.8u, 2u) \dots z_4;$ 
endfig;

beginfig(140);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 3u);$ 

```

```

 $z_3 = (2u, 0);$ 
 $z_4 = .5[z_2, z_3];$ 
path  $p;$ 
 $p = z_1 -- z_2 -- z_3 -- cycle;$ 
draw  $p;$ 
draw  $z_1 -- z_4;$ 
 $draw\_marked(z_2 -- z_4, 1);$ 
 $draw\_marked(z_4 -- z_3, 1);$ 
 $draw\_marked(z_1 -- z_4, 1);$ 
endfig;

beginfig(141);
 $z_1 = (0, u);$ 
 $z_2 = (3u, u);$ 
 $z_3 = (.5u, u);$ 
 $z_4 = (2.5u, u);$ 
 $z_5 = (.5u, 0);$ 
 $z_6 = (2.5u, 0);$ 
draw  $z_1 -- z_2;$ 
draw  $z_3 -- z_5$  dashed evenly;
draw  $z_4 -- z_6$  dashed evenly;
draw  $(z_1 -- z_2)$  shifted  $(0, -u);$ 
dotlabel(btex  $$$$  etex,  $z_3$ );
dotlabel(btex  $$$$  etex,  $z_4$ );
endfig;

beginfig(142);
 $z_1 = (0, u);$ 
 $z_2 = (3u, u);$ 
 $z_3 = (.5u, u);$ 
 $z_4 = (2.5u, u);$ 
 $z_5 = (.5u, 0);$ 
 $z_6 = (2.5u, 0);$ 
draw  $z_1 -- z_2$  dashed evenly;
draw  $z_3 -- z_5;$ 
draw  $z_4 -- z_6;$ 
draw  $(z_1 -- z_2)$  shifted  $(0, -u);$ 
dotlabel(btex  $$$$  etex,  $z_3$ );
dotlabel(btex  $$$$  etex,  $z_4$ );
label  $rt$ (btex  $\$h\$$  etex,  $.5[z_3, z_5]$ );
label  $rt$ (btex  $\$h\$$  etex,  $.5[z_4, z_6]$ );
endfig;

beginfig(144);
 $z_1 = (0, 0);$ 
 $z_2 = (1.5u, u);$ 
 $z_3 = (3u, 0);$ 
 $z_4 = (1.5u, -u);$ 
draw  $z_1 -- z_2 -- z_3 -- z_4 -- cycle;$ 
 $draw\_marked(z_1 -- z_2, 1);$ 
 $draw\_marked(z_2 -- z_3, 1);$ 
 $draw\_marked(z_3 -- z_4, 1);$ 
 $draw\_marked(z_4 -- z_1, 1);$ 
endfig;

```

```

beginfig(145);
 $z_1 = (0, 0);$ 
 $z_2 = (1.5u, u);$ 
 $z_3 = (3u, 0);$ 
 $z_4 = (1.5u, -u);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw  $z_1$  --  $z_3$ ;
draw  $z_2$  --  $z_4$ ;
endfig;

```

```

beginfig(146);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (2u, 2u);$ 
 $z_4 = (2u, 0);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw_marked( $z_1$  --  $z_2$ , 1);
draw_marked( $z_2$  --  $z_3$ , 1);
draw_marked( $z_3$  --  $z_4$ , 1);
draw_marked( $z_4$  --  $z_1$ , 1);
mark_rt_angle( $z_4$ ,  $z_1$ ,  $z_2$ );
mark_rt_angle( $z_1$ ,  $z_2$ ,  $z_3$ );
mark_rt_angle( $z_2$ ,  $z_3$ ,  $z_4$ );
mark_rt_angle( $z_3$ ,  $z_4$ ,  $z_1$ );
endfig;

```

```

beginfig(147);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (2u, 2u);$ 
 $z_4 = (2u, 0);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw  $z_1$  --  $z_3$ ;
endfig;

```

```

beginfig(148);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = (1.5u, 2u);$ 
 $z_4 = (1.5u, 0);$ 
 $z_5 = (0, 2.5u);$ 
 $z_6 = (2u, 0);$ 
draw  $z_1$  --  $z_2$  --  $z_3$  --  $z_4$  -- cycle;
draw  $z_2$  --  $z_5$ ;
draw  $z_4$  --  $z_6$ ;
label lft(btex  $\$Q\$$  etex,  $z_2$ );
label urt(btex  $\$X\$$  etex,  $z_3$ );
label bot(btex  $\$P\$$  etex,  $z_4$ );
endfig;

```

```

beginfig(149);
path  $p$ ,  $q$ ,  $e$ ;
 $p = \text{fullcircle scaled } 2u;$ 
 $q = p$  shifted  $(1.5u, 0);$ 
 $z_1 = p$  intersectionpoint  $q$ ;

```



```

e = subpath(7, 8) of p;
z2 = e intersectionpoint q;
z3 = (0, 0);
z4 = z3 shifted (1.5u, 0);
draw z3 -- z1 -- z4 -- z2 -- cycle dashed evenly;
draw p;
draw q;
pickup pencircle scaled 0.14u;
dotlabel(btex $$ etex, z1);
dotlabel(btex $$ etex, z2);
dotlabel(btex $$ etex, z3);
dotlabel(btex $$ etex, z4);
endfig;

beginfig(151);
z11 = (-.5u, 0);
z22 = (4u, 0);
z33 = z11 shifted (0, 2u);
z44 = z22 shifted (0, 2u);
z1 = (0, .2u); z2 = z1 shifted (u, 2u); z3 = z2 shifted (2u, -u); z4 = z1 shifted (2u, -u);
z5 = whatever[z1, z2] = whatever[z33, z44];
z6 = whatever[z2, z3] = whatever[z33, z44];
z7 = whatever[z3, z4] = whatever[z11, z22];
z8 = whatever[z1, z4] = whatever[z11, z22];
z9 = whatever[z5, z7] = whatever[z6, z8];
draw z11 -- z22;
draw z33 -- z44;
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z5 -- z7;
draw z6 -- z8;
mark_ang(z8, z9, z7, angle_radius);
pickup pencircle scaled .14u;
dotlabel(btex $$ etex, z5);
dotlabel(btex $$ etex, z6);
dotlabel(btex $$ etex, z7);
dotlabel(btex $$ etex, z8);
dotlabel(btex $$ etex, z9);
label bot(btex $45$ etex, z9 shifted (0, -.5u));
endfig;

beginfig(152);
z1 = (0, 0);
z2 = (2u, 0);
z3 = z2 rotated 60;
draw z1 -- z2 -- z3 -- cycle;
mark_ang(z2, z1, z3, angle_radius);
mark_ang(z3, z2, z1, angle_radius);
mark_ang(z1, z3, z2, angle_radius);
draw_marked(z1 -- z2, 1);
draw_marked(z2 -- z3, 1);
draw_marked(z1 -- z3, 1);
endfig;

beginfig(153);
path p;

```

```


$p = \text{fullcircle scaled } 4u;$   

draw  $p;$   

dotlabel(btex  $\$ \$ \text{etex}$ ,  $(0, 0)$ );  

endfig;


```

```

beginfig(154);
 $z_1 = (0, 0);$ 
 $z_2 = (2u, 0);$ 
 $z_3 = z_2 \text{ rotated } 60;$ 
path  $p, q, e, f;$ 
 $q = z_1 \text{ -- } z_2 \text{ -- } z_3 \text{ -- cycle};$ 
 $p = \text{fullcircle scaled } 4u;$ 
 $z_4 = p \text{ intersectionpoint } q;$ 
 $e = \text{subpath}(1, 2) \text{ of } p;$ 
 $f = \text{subpath}(7.5, 10) \text{ of } p;$ 
 $z_5 = e \text{ intersectionpoint } q;$ 
draw  $f;$ 
draw  $q;$ 
label bot(btex  $\$r\$ \text{etex}$ ,  $.5[z_1, z_2]$ );
label lft(btex  $\$r\$ \text{etex}$ ,  $.5[z_2, z_3]$ );
label ulft(btex  $\$r\$ \text{etex}$ ,  $.5[z_1, z_3]$ );
pickup pencircle scaled  $0.14u;$ 
dotlabel(btex  $\$ \$ \text{etex}$ ,  $z_1$ );
dotlabel(btex  $\$ \$ \text{etex}$ ,  $z_2$ );
dotlabel(btex  $\$ \$ \text{etex}$ ,  $z_3$ );
endfig;
```

```

beginfig(155);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = z_2 \text{ shifted } (3u, 0);$ 
 $z_4 = z_1 \text{ shifted } (3u, 0);$ 
 $z_5 = z_2 \text{ shifted } (u, u);$ 
 $z_6 = z_3 \text{ shifted } (u, u);$ 
 $z_7 = z_4 \text{ shifted } (u, u);$ 
draw  $z_1 \text{ -- } z_2 \text{ -- } z_3 \text{ -- } z_4 \text{ -- cycle};$ 
draw  $z_2 \text{ -- } z_5 \text{ -- } z_6 \text{ -- } z_3;$ 
draw  $z_6 \text{ -- } z_7 \text{ -- } z_4 \text{ -- } z_6 \text{ -- } z_2 \text{ -- } z_4;$ 
endfig;
```

```

beginfig(156);
 $z_1 = (0, 0);$ 
 $z_2 = (0, 2u);$ 
 $z_3 = z_2 \text{ shifted } (3u, 0);$ 
 $z_4 = z_1 \text{ shifted } (3u, 0);$ 
 $z_5 = z_2 \text{ shifted } (u, u);$ 
 $z_6 = z_3 \text{ shifted } (u, u);$ 
 $z_7 = z_4 \text{ shifted } (u, u);$ 
draw  $z_1 \text{ -- } z_2 \text{ -- } z_3 \text{ -- } z_4 \text{ -- cycle};$ 
draw  $z_2 \text{ -- } z_5 \text{ -- } z_6 \text{ -- } z_3;$ 
draw  $z_2 \text{ -- } z_4 \text{ -- } z_6 \text{ -- } z_7 \text{ -- } z_4 \text{ -- } z_6;$ 
draw  $z_2 \text{ -- } z_6 \text{ dashed evenly};$ 
endfig;
```

```

beginfig(157);
```

```

z1 = (0, 0);
z2 = (0, 2.5u);
z3 = z2 shifted (2.5u, 0);
z4 = z1 shifted (2.5u, 0);
z5 = z4 rotated 30;
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z2 -- z5 -- z1;
draw z3 -- z5 -- z4 dashed evenly;
label llft(btex  $A$  etex, z1);
label ulft(btex  $B$  etex, z2);
label urt(btex  $C$  etex, z3);
label lrt(btex  $D$  etex, z4);
label lft(btex  $M$  etex, z5 shifted (-.2u, 0));
draw_marked(z1 -- z2, 1);
draw_marked(z2 -- z3, 1);
draw_marked(z3 -- z4, 1);
draw_marked(z4 -- z1, 1);
draw_marked(z1 -- z5, 1);
draw_marked(z2 -- z5, 1);
endfig;

```

```

beginfig(158);
z1 = (0, 0);
z2 = (0, 2.5u);
z3 = z2 shifted (2.5u, 0);
z4 = z1 shifted (2.5u, 0);
z5 = (1.25u, 0) rotated 75;
draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z2 -- z5 -- z1;
draw z3 -- z5 -- z4 dashed evenly;
label llft(btex  $A$  etex, z1);
label ulft(btex  $B$  etex, z2);
label urt(btex  $C$  etex, z3);
label lrt(btex  $D$  etex, z4);
label rt(btex  $L$  etex, z5 shifted (.5u, 0));
mark_ang(z5, z1, z2, angle_radius);
mark_ang(z1, z2, z5, angle_radius);
mark_ang(z4, z5, z3, angle_radius);
endfig;

```

```

beginfig(159);
z1 = (0, 0);
z2 = (3u, 0);
z3 = z2 rotated 60;
z4 = 2/3[z1, z2];
z5 = 2/3[z2, z3];
z6 = 2/3[z3, z1];
draw z1 -- z2 -- z3 -- cycle;
draw z4 -- z5 -- z6 -- cycle dashed evenly;
endfig;

```

```

beginfig(160);
z1 = (0, 0);
z2 = (3u, 0);

```

```

z3 = (2u, 2.5u);
z4 = .5[z1, z2];
z5 = .5[z2, z3];
z6 = .5[z3, z1];
draw z1 -- z2 -- z3 -- cycle;
draw z4 -- z5 -- z6 dashed evenly;
label llft(btex  $A$  etex, z1);
label ulft(btex  $B$  etex, z3);
label lrt(btex  $C$  etex, z2);
label urt(btex  $M$  etex, z5);
endfig;

```

```

beginfig(161);
z1 = (0, 0);
z2 = (3u, 0);
z3 = (2u, 2.5u);
z4 = .5[z1, z2];
z5 = .5[z2, z3];
z6 = .5[z3, z1];
draw z1 -- z2 -- z3 -- cycle;
draw z4 -- z5 -- z6;
label llft(btex  $A$  etex, z1);
label ulft(btex  $B$  etex, z3);
label lrt(btex  $C$  etex, z2);
label urt(btex  $M$  etex, z5);
label ulft(btex  $K$  etex, z6);
label bot(btex  $L$  etex, z4);
mark_ang(z1, z3, z2, 4pt);
mark_ang(z4, z5, z2, 4pt);
mark_angtwice(z3, z5, z6, 4pt);
mark_angtwice(z3, z2, z1, 4pt);
draw_marked(z3 -- z5, 1);
draw_marked(z5 -- z2, 1);
endfig;

```

```

beginfig(163);
z1 = (0, 0);
z2 = (3u, 0);
z3 = (u, 2.5u);
z4 = .5[z1, z2];
z5 = .5[z2, z3];
z6 = .5[z3, z1];
draw z1 -- z2 -- z3 -- cycle;
draw z4 -- z5 -- z6 -- cycle;
endfig;

```

```

beginfig(164);
z1 = (0, 0);
z2 = (.5u, 2u);
z3 = (3u, 1.5u);
z4 = (3.5u, -1.5u);
z5 = .5[z1, z2];
z6 = .5[z2, z3];
z7 = .5[z3, z4];
z8 = .5[z4, z1];

```

```

draw z1 -- z2 -- z3 -- z4 -- cycle;
draw z5 -- z6 -- z7 -- z8 -- cycle dashed evenly;
draw z1 -- z3;
draw z2 -- z4;
endfig;

beginfig(165);
z1 = (0, 0);
z2 = (u, 2.5u);
z3 = (2u, 0);
z4 = (u, -2.5u);
z12 = .5[z1, z2];
z23 = .5[z2, z3];
z34 = .5[z3, z4];
z41 = .5[z4, z1];
z11 = (0, 2.5u); z22 = (2u, 2.5u); z33 = (2u, -2.5u); z44 = (0, -2.5u);
z5 = (u, -5u); z6 = z5 shifted (0, 2u); z7 = z6 shifted (2u, 0); z8 = z5 shifted (2u, 0);
z56 = .5[z5, z6];
z67 = .5[z6, z7];
z78 = .5[z7, z8];
z85 = .5[z8, z5];
path p, q;
p = z1 -- z2 -- z3 -- z4 -- cycle;
q = (z11 -- z22 -- z33 -- z44 -- cycle) shifted (3u, 0);
draw p;
draw z12 -- z23 -- z34 -- z41 -- cycle dashed evenly;
draw p shifted (3u, 0) dashed evenly;
draw q;
draw z5 -- z6 -- z7 -- z8 -- cycle;
draw z56 -- z67 -- z78 -- z85 -- cycle dashed evenly;
endfig;
end

```